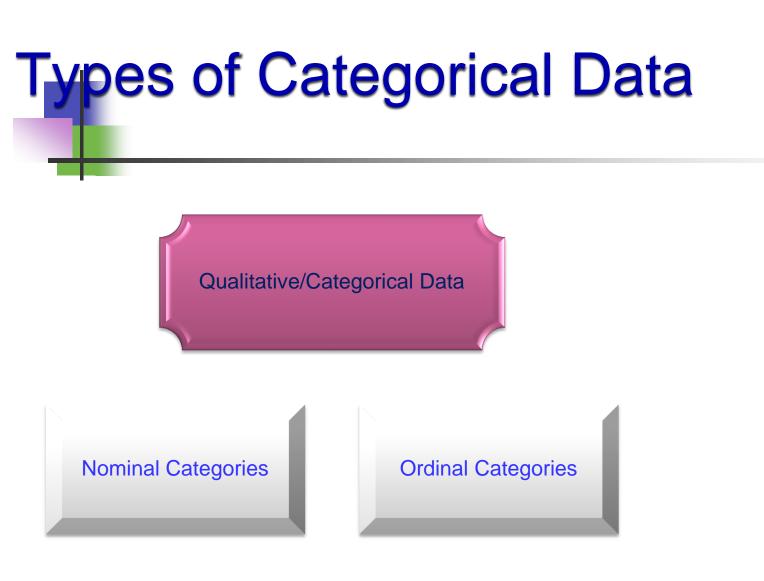
Statistical tests to observe the statistical significance of qualitative variables (Chisquare, Fisher's exact & Mac Nemar's chisquare tests)

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# **Objectives:**

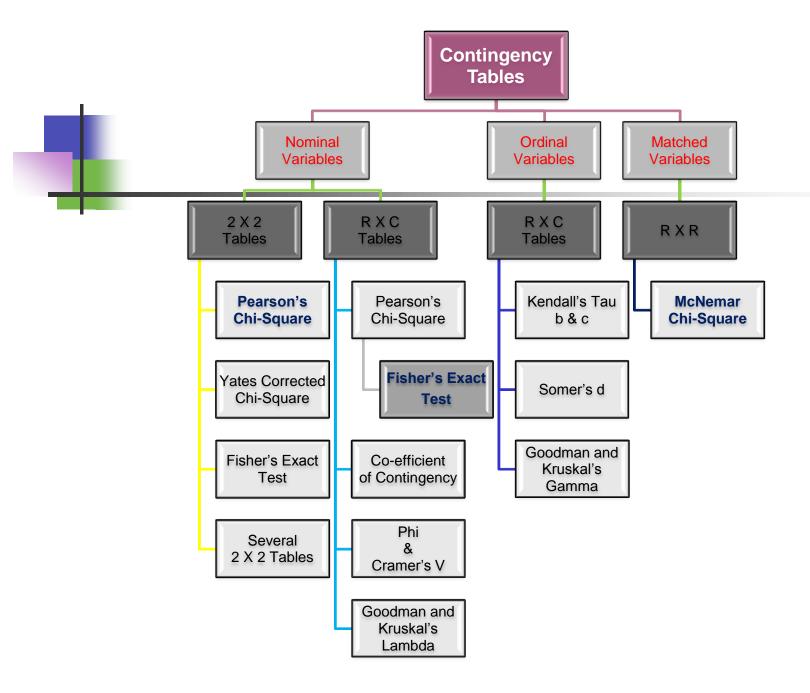
- (1) Able to understand the factors to apply for the choice of statistical tests in analyzing the data.
- (2) Able to apply appropriately Chisquare test, Fisher's exact test & Macnemar's Chi-square test.
- (3) Able to interpret the findings of the analysis using these three tests.



# Types of Analysis for Categorical Data

Type of Analysis

Descriptive Rate and Ratio Analytic Confidence Interval and Test of Significance



Choosing the appropriate Statistical test

Based on the three aspects of the data
Types of variables
Number of groups being compared &
Sample size

# Statistical test (cont.)

Chi-square test:

Study variable: Qualitative(Categorical)

Outcome variable: Qualitative(Categorical)

<u>Comparison:</u> two or more proportions

Sample size: >30

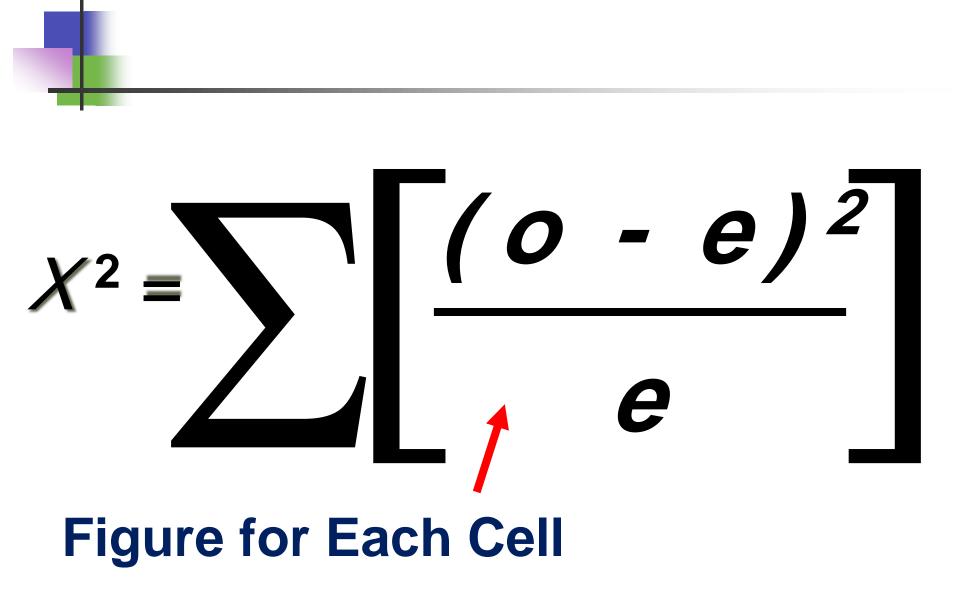
Expected frequency: > 5



To find out whether the association between two categorical variables are statistically significant

## **Null Hypothesis**

There is no association between two variables



. The summation is over all cells of the contingency table consisting of r rows and c columns

- 2. O is the observed frequency
- 3. È is the expected frequency

$$\hat{E} = \frac{ \left( \begin{array}{c} \text{total of row in} \\ \text{which the cell lies} \end{array} \right) \cdot \left( \begin{array}{c} \text{total of column in} \\ \text{which the cell lies} \end{array} \right) }{ (\text{total of all cells}) }$$

reject 
$$H_0$$
 if  $\chi^2 > \chi^2_{.\alpha,df}$   
where df = (r-1)(c-1)  $\chi^2 = \sum \frac{(O-E)^2}{E}$ 

4. The degrees of freedom are df = (r-1)(c-1)

# Requirements

- Prior to using the chi square test, there are certain requirements that must be met.
  - The data must be in the form of frequencies counted in each of a set of categories. Percentages cannot be used.
  - The total number observed must be exceed 20.

# Requirements

- The expected frequency under the H<sub>0</sub> hypothesis in any one fraction must not normally be less than 5.
- All the observations must be independent of each other. In other words, one observation must not have an influence upon another observation.

## **APPLICATION OF CHI-SQUARE TEST**

## TESTING INDEPENDCNE (or ASSOCATION)

## TESTING FOR HOMOGENEITY

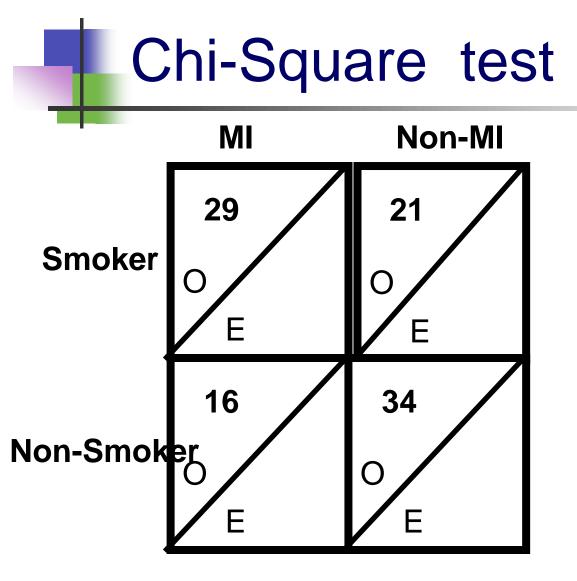
TESTING OF GOODNESS-OF-FIT

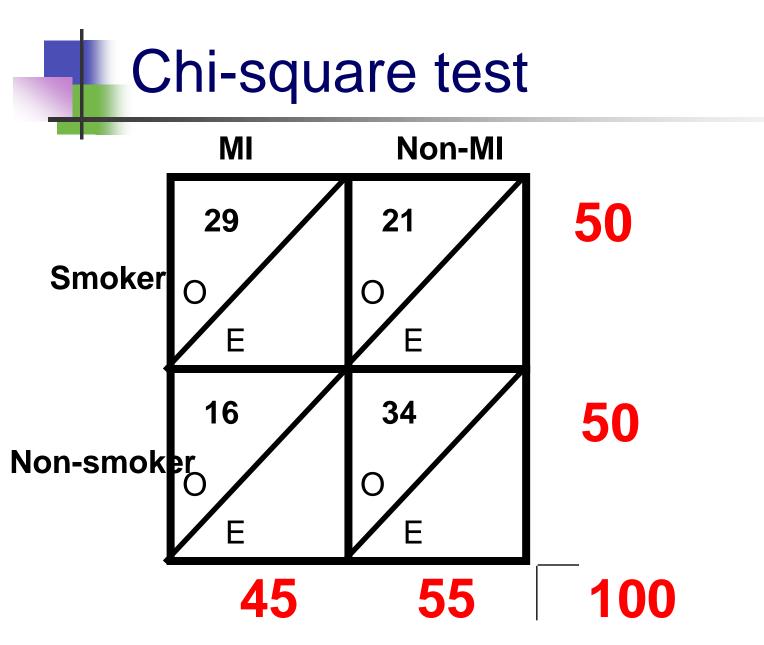
# **Chi-square test**

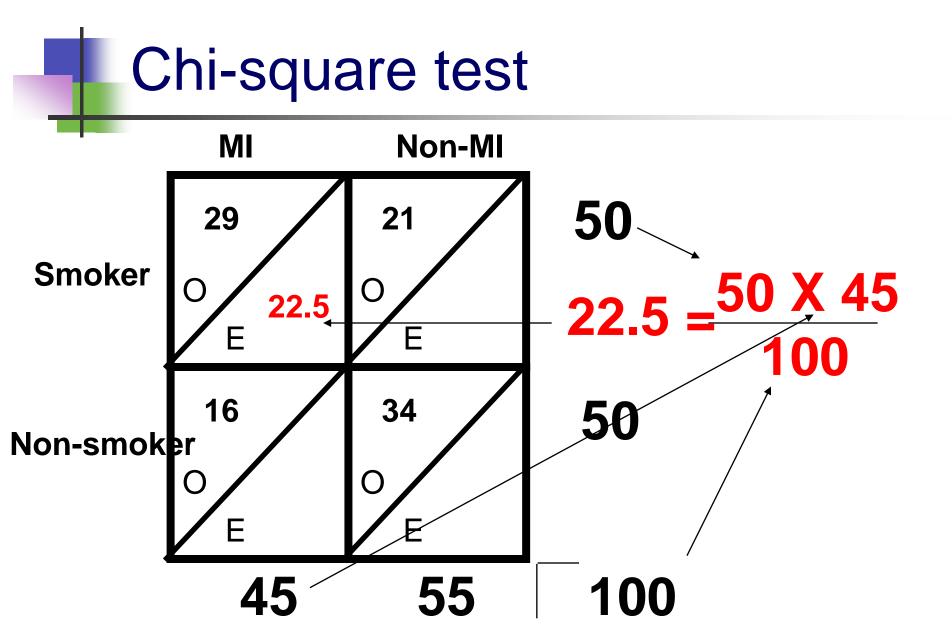
### Objective : Smoking is a risk factor for MI

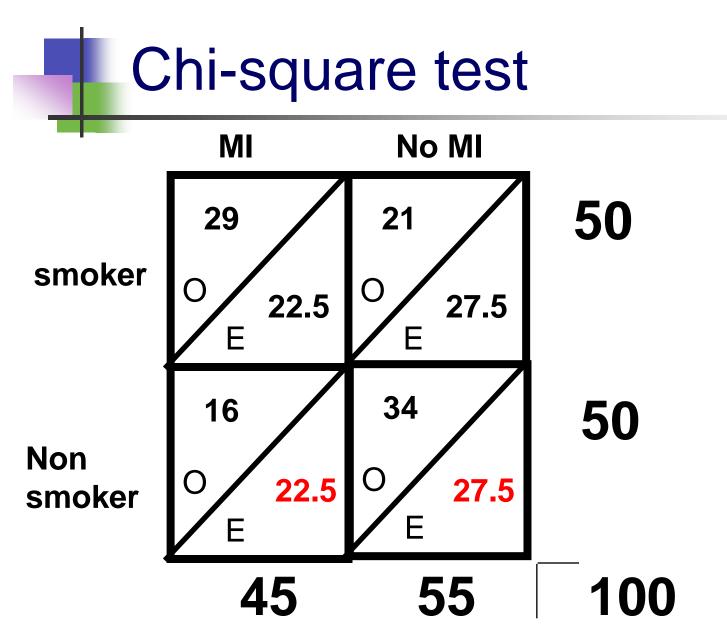
# Null Hypothesis: Smoking does not cause MI

	D (MI)	No D( No MI)	Total
Smokers	29	21	50
Non-smokers	16	34	50
Total	45	55	100









# **Chi-Square**

Degrees of Freedom df = (r-1) (c-1)= (2-1) (2-1) = 1

Critical Value (Table A.6) = 3.84

 $X^2 = 6.84$ 

Calculated value(6.84) is greater than critical (table) value (3.84) at 0.05 level with 1 d.f.f

Hence we reject our Ho and conclude that there is highly statistically significant association between smoking and MI.

#### Background:

Contradictory opinions:

 1. A diabetic's risk of dying after a first heart attack is the same as that of someone without diabetes. There is no association between diabetes and heart disease.

VS.

- 2. Diabetes takes a heavy toll on the body and diabetes patients often suffer heart attacks and strokes or die from cardiovascular complications at a much younger age.
- So we use hypothesis test based on the latest data to see what's the right conclusion.
- There are a total of 5167 patients, among which <u>1131 patients are non-diabetics</u> and <u>4036 are diabetics</u>. Among the non-diabetic patients, <u>42%</u> of them had their blood pressure properly controlled (therefore it's <u>475 of 1131</u>). While among the diabetic patients only <u>20%</u> of them had the blood pressure controlled (therefore it's <u>807 of 4036</u>).

#### Data

	Controlled	Uncontrolled	Total
Non-diabetes	475	656	1131
Diabetes	807	3229	4036
Total	1282	3885	5167

Data:

Diabetes: 1=Not have diabetes, 2=Have Diabetes Control: 1=Controlled, 2=Uncontrolled

**DIABETES \* CONTROL Crosstabulation** 

		CONTROL		
		1.00	2.00	Total
DIABETES	1.00	475	656	1131
	2.00	807	3229	4036
Total		1282	3885	5167

Count

			CON	FROL	
			1.00	2.00	Total
DIABETES	1.00	Count	475	656	1131
		% within DIABETES	42.0%	58.0%	100.0%
		% within CONTROL	37.1%	16.9%	21.9%
		% of Total	9.2%	12.7%	21.9%
	2.00	Count	807	3229	4036
		% within DIABETES	20.0%	80.0%	100.0%
		% within CONTROL	62.9%	83.1%	78.1%
		% of Total	15.6%	62.5%	78.1%
Total		Count	1282	3885	5167
		% within DIABETES	24.8%	75.2%	100.0%
		% within CONTROL	100.0%	100.0%	100.0%
		% of Total	24.8%	75.2%	100.0%

#### **DIABETES \* CONTROL Crosstabulation**

Hypothesis test:

H<sub>0</sub>: There is no association between diabetes and heart disease. (or) Diabetes and heart disease are independent.

#### VS

H<sub>A</sub>: There is an association between diabetes and heart disease. (or) Diabetes and heart disease are dependent.

--- Assume a significance level of 0.05

#### SPSS Output

	Value	df	Asymp. Sig. (2-sided)	Exact Sig. (2-sided)	Exact Sig. (1-sided)
Pearson Chi-Square	229.268 <sup>b</sup>	1	.000		
Continuity Correction	228.091	1	.000		
Likelihood Ratio	212.149	1	.000		
Fisher's Exact Test				.000	.000
Linear-by-Linear Association	229.224	1	.000		
N of Valid Cases	5167				

#### **Chi-Square Tests**

- a. Computed only for a 2x2 table
- b. 0 cd ls (.0%) have expected count less than 5. The minimum expected count is 280.62.

- ---The computer gives us a Chi-Square Statistic of 229.268
- ---The computer gives us a p-value of .000 (<0.0001)
- --- Because our p-value is less than alpha, we would reject the null hypothesis.
- --- There is sufficient evidence to conclude that there is an association between diabetes and heart disease.

Chi- square test

# Find out whether the gender is equally distributed among each age group

		Age		
Gender	<30	30-45	>45	Total
Male	60 (60)	20 (30)	40 (30)	120
Female	40 (40)	30 (20)	10 (20)	80
Total	100	50	50	200

## **Test for Homogeneity (Similarity)**

To test similarity between frequency distribution or group. It is used in assessing the similarity between nonresponders and responders in any survey

Age (yrs)	Responders	Non-responders	Total
<20	76 (82)	20 (14)	96
20 - 29	288 (289)	50 (49)	338
30-39	312 (310)	51 (53)	363
40-49	187 (185)	30 (32)	217
>50	77 (73)	9 (13)	86
Total	940	160	1100



<u>Study variable:</u> Qualitative(Categorical)

<u>Outcome variable:</u> Qualitative(Categorical)

<u>Comparison:</u> two proportions

<u>Sample size: < 30</u>



The following data relate to suicidal feelings in samples of psychotic and neurotic patients:

	Psychotics	Neurotics	Total
Suicidal feelings	2	6	8
No suicidal feelings	18	14	32
Total	20	20	40

# Example

## The following data compare malocclusion of teeth with method of feeding infants.

	Normal teeth	Malocclusion
Breast fed	4	16
Bottle fed	1	21

# Fisher's Exact Test:

The method of Yates's correction was useful when manual calculations were done. Now different types of statistical packages are available. Therefore, it is better to use Fisher's exact test rather than Yates's correction as it gives exact result.

Fisher's Exact Test = 
$$\frac{R_1!R_2!C_1!C_2!}{n!a!b!c!d!}$$

# What to do when we have a paired samples and both the exposure and outcome variables are qualitative variables (Binary).

## Macnemar's test: (for paired samples)

Study variable: Qualitative (categorical)

<u>Outcome variable:</u> Qualitative(categorical)

<u>Comparison:</u> two proportions

Sample size: Any

## Problem

A researcher has done a matched casecontrol study of endometrial cancer (cases) and exposure to conjugated estrogens (exposed).

In the study cases were individually matched 1:1 to a non-cancer hospitalbased control, based on age, race, date of admission, and hospital.



## Situation:

Two paired binary variables that form a particular type of 2 x 2 table

e.g. matched case-control study or cross-over trial



	Cases	Controls	Total
Exposed	55	19	74
Not exposed	128	164	292
Total	183	183	366

• can't use a chi-squared test - observations are not independent - they're paired. • we must present the 2 x 2 table differently • each cell should contain a count of the number of pairs with certain criteria, with the columns and rows respectively referring to each of the subjects in the matched pair

 the information in the standard 2 x 2 table used for unmatched studies is insufficient because it doesn't say who is in which pair

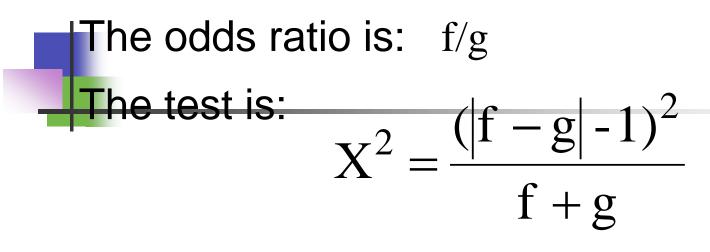
- ignoring the matching



	Co		
Cases	Exposed	Not exposed	Total
Exposed	12	43	55
Not exposed	7	121	128
Total	19	164	183

We construct a matched 2 x 2 table:					
	Cc	ontrols			
Cases	Exposed	Not exposed	Total		
Exposed	е	f	e+f		
Not exposed	g	h	g+h		
Total	e+g	f+h	n		

# Formula



Compare this to the  $\chi^2$  distribution on 1 df

$$X^{2} = \frac{(|43-7|-1)^{2}}{43+7} = \frac{1225}{50} = 24.5$$

P <0.001, Odds Ratio = 43/7 = 6.1  $p_1 - p_2 = (55/183) - (19/183) = 0.197$  (20%) s.e. $(p_1 - p_2) = 0.036$ 95% CI: 0.12 to 0.27 (or 12% to 27%)

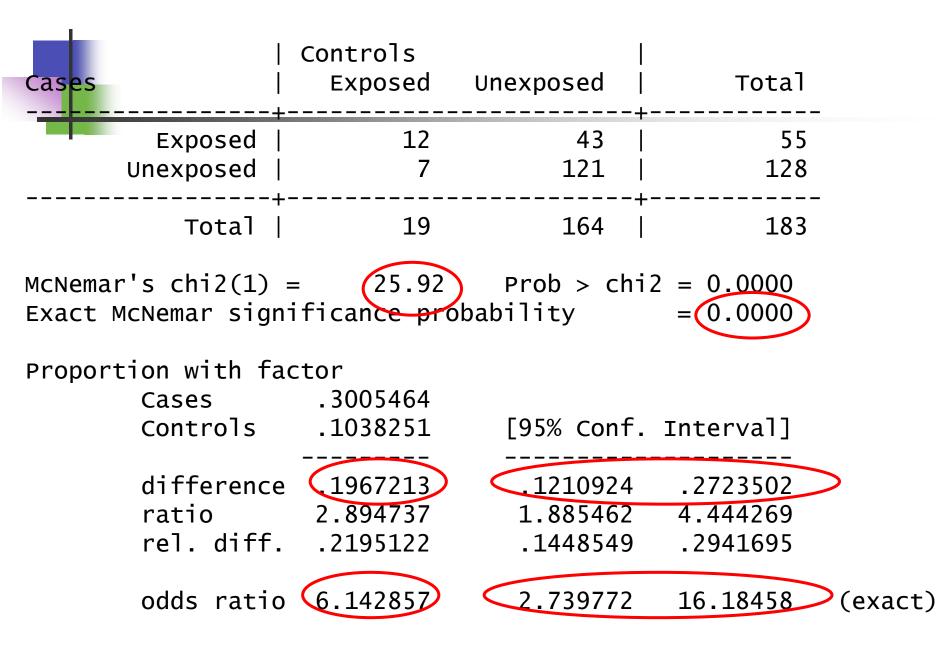
#### Degrees of Freedom *df* = (r-1) (c-1) = (2-1) (2-1) =1

- Critical Value (Table A.6) = 3.84
- $X^2 = 25.92$
- Calculated value(25.92) is greater than critical (table) value (3.84) at 0.05 level with 1 d.f.f
- Hence we reject our Ho and conclude that there is highly statistically significant association between Endometrial cancer and Estrogens.

#### Two-tailed critical ratios of $\chi^2$

Degrees of freedom df	. 10	.05	.02	.01
1	2.706	3.841	5.412	6,635
2	4.605	5.991	7.824	9,210
3	6.251	7.815	9.837	11,341
4	7.779	9.488	11.668	13,277
5	9.236	11.070	13.388	15,086
6	10,645	12.592	15.033	16.812
7	12,017	14.067	16.622	18.475
8	13,362	15.507	18.168	20.090
9	14,684	16.919	19.679	21.666
10	15,987	18.307	21.161	23.209
11	17.275	19.675	22.618	24.725
12	18.549	21.026	24.054	26.217
13	19.812	22.362	25.472	27.688
14	21.064	23.685	26.873	29.141

# Stata Output



# In Conclusion !

When both the study variables and outcome variables are categorical (Qualitative):

Apply (i) Chi square test (ii) Fisher's exact test (Small samples) (iii) Mac nemar's test (for paired samples)